

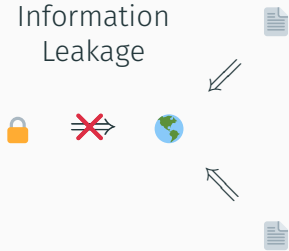
Structural Information Flow: A Fresh Look at Types for Non-Interference

Hemant Gouni (with Frank Pfenning & Jonathan Aldrich)

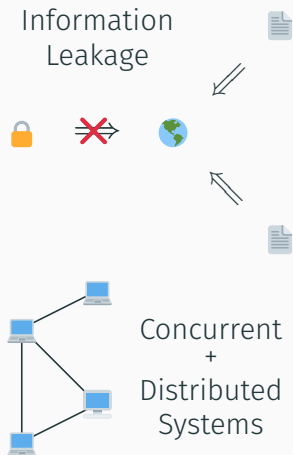
October 20, 2025

Information Flow Tracks *Dependencies*

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Information Flow Tracks *Dependencies*

Information
Leakage



Concurrent
+
Distributed
Systems

Program Slicing

Information Flow Tracks *Dependencies*

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Build Systems 

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Controlling Opaque Definitions

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Lineage Tracking in CAD 

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Controlling Opaque Definitions

Lineage Tracking in CAD

...and **much** more!!

How to Reinvent Our Approach From Scratch 🧑🔧

A Familiar Friend: Parametric Polymorphism

```
val id :  $\alpha$  ->  $\alpha$ 
```

```
val snd :  $\alpha$  ->  $\beta$  ->  $\alpha$ 
```

```
val map : ( $\alpha$  ->  $\beta$ ) -> list  $\alpha$  -> list  $\beta$ 
```

A Familiar Friend: Parametric Polymorphism

`val id : α -> α`



`val snd : α -> β -> α`

`val map : (α -> β) -> list α -> list β`

A Familiar Friend: Parametric Polymorphism

val id : $\alpha \rightarrow \alpha$



val snd : $\alpha \rightarrow \beta \rightarrow \alpha$



val map : $(\alpha \rightarrow \beta) \rightarrow \text{list } \alpha \rightarrow \text{list } \beta$

A Familiar Friend: Parametric Polymorphism

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What about `incr : int -> int`?

A Familiar Friend: Parametric Polymorphism

`val id : $\alpha \rightarrow \alpha$`

`val snd : $\alpha \rightarrow \beta \rightarrow \alpha$`

`val map : ($\alpha \rightarrow \beta$) \rightarrow list $\alpha \rightarrow$ list β`

What about `incr : int \rightarrow int`?

Insight 1

Separate **data abstraction** from **information flow**.

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Relaxing Parametricity

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Idea: Tag types with *dependency variables* α

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Result: `incr : α int -> α int`

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Result: $\text{incr} : \alpha \text{ int} \rightarrow \alpha \text{ int}$



Relaxing Parametricity

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Result: $\text{incr} : \alpha \text{ int} \rightarrow \alpha \text{ int}$



What about $\text{add} : \alpha \text{ int} \rightarrow \beta \text{ int} \rightarrow \boxed{?} \text{ int}$?

Relaxing Parametricity

Insight 1


Separate data abstraction from information flow.

Idea: Tag types with *dependency variables* α

Result: $\text{incr} : \alpha \text{ int} \rightarrow \alpha \text{ int}$

A black line connects the α in the input type to the α in the output type, indicating that the output depends on the input's dependency variable.

What about $\text{add} : \alpha \text{ int} \rightarrow \beta \text{ int} \rightarrow \boxed{?} \text{ int}?$

Two dependency arrows are shown: a pink arrow from the first α to the β , and a blue arrow from the β to the boxed question mark. This indicates that the final result depends on both input types.

Relaxing Parametricity

Insight 1


Separate **data abstraction** from **information flow**.

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Result: $\text{incr} : \alpha \text{ int} \rightarrow \alpha \text{ int}$



What about $\text{add} : \alpha \text{ int} \rightarrow \beta \text{ int} \rightarrow \boxed{?} \text{ int?}$



Insight 2

Track **sets of dependencies** in types.

Generalizing to Dependency Sets

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Result: $\text{add} : [\alpha] \text{ int} \rightarrow [\beta] \text{ int} \rightarrow [\alpha \beta] \text{ int}$

```
graph LR; A["[α] int"] -- red --> R["[α β] int"]; B["[β] int"] -- blue --> R;
```

Generalizing to Dependency Sets

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graph LR; A["[α] int"] -- red --> R["[α β] int"]; B["[β] int"] -- blue --> R;
```

Let's work a more interesting example of information flow!

A Password Checker

```
let pass : [pwd] string = "katya"
```

```
let check : [ $\alpha$ ] string -> [ $\alpha$  pwd] bool =  
  fun attempt -> attempt == pass
```

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Our checker is too conservative!

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The conventional solution to this issue is *declassification*...

A Password Checker

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A Password Checker

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Our checker is too conservative!

The conventional solution to this issue is *declassification*...

...which *subverts* the type system.

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Non-interference says dependency tracking must be **faithful**; declassification **opposes** it.

[Non-interference] is too strict to be usable in realistic programs.

— Wikipedia (Information Flow)

Non-interference says dependency tracking must be **faithful**; declassification **opposes** it.

Noninterference is over-restrictive for programs with intentional information release (average salary, information purchase and password checking programs are flatly rejected by noninterference).

— Sabelfeld and Sands 07

Non-interference says dependency tracking must be **faithful**; declassification **opposes** it.

We resolve this conflict: the tools we've **already introduced** suffice for realistic programs.

Declassification for Free 🩹

Step 0: Wishful Thinking

```
signature PasswordChecker = sig
```

```
end
```

```
open PasswordChecker as pc
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  pass : [pwd] string
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open PasswordChecker as pc
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```
let _ : [pwd] string = pc.pass ++ "arren"
```

Step 0: Wishful Thinking

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signature PasswordChecker = sig
  dependency pwd

  pass : [pwd] string
  check : [ $\alpha$ ] string -> [ $\alpha$ ] bool

end
```

```
open PasswordChecker as pc
```

```
let _ : [pwd] string = pc.pass ++ "arren"
let _ : [ ] bool = pc.check "nemmerle"
```

Step 0: Wishful Thinking

```
signature PasswordChecker = sig
  dependency pwd

  pass : [pwd] string
  check : [ $\alpha$ ] string -> [ $\alpha$ ] bool
  encrypt : [pwd  $\alpha$ ] string -> [ $\alpha$ ] string
end
```

```
open PasswordChecker as pc
```

```
let _ : [pwd] string = pc.pass ++ "arren"
let _ : [ ] bool = pc.check "nemmerle"
let _ : [ ] string = pc.encrypt pc.pass
```

Step 1: Expose Lurking Quantifiers 🧐

id : $\alpha \rightarrow \alpha$

map : $(\alpha \rightarrow \beta) \rightarrow \text{list } \alpha \rightarrow \text{list } \beta$

add : $[\alpha] \text{ int} \rightarrow [\beta] \text{ int} \rightarrow [\alpha \beta] \text{ int}$

Step 1: Expose Lurking Quantifiers 🧐

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Insight 3

Construct `exists α` from `forall α` + higher-order functions

Step 1: Expose Lurking Quantifiers 🧐

`id : forall α . $\alpha \rightarrow \alpha$`

`map : forall $\alpha \beta$. ($\alpha \rightarrow \beta$) \rightarrow list $\alpha \rightarrow$ list β`

`add : forall $\alpha \beta$. [α] int \rightarrow [β] int \rightarrow [$\alpha \beta$] int`

Insight 3

Construct `exists α` from `forall α` + higher-order functions

Existentials are better known as *modules* or *classes*!*

*(roughly)

Step 2: Dependency Abstraction 🍷

```
signature Queue = sig
```

```
  type t
```

```
  enqueue : int -> t -> t
```

```
  dequeue : t -> t * int
```

```
end
```

```
structure naive_queue : Queue = struct
```

```
  type t = List int
```

```
  enqueue x q = Cons(x, q)
```

```
  dequeue q = match q with ...
```

```
end
```

Step 2: Dependency Abstraction 🍷

```
signature Queue = sig
```

```
  type t  Existentially Quantified!
```

```
  enqueue : int -> t -> t
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  dequeue : t -> t * int
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```
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  enqueue x q = Cons(x, q)
```

```
  dequeue q = match q with ...
```

```
end
```

Step 2: Dependency Abstraction 🤖

client view

```
signature Queue = sig
  type t

  enqueue : int -> t -> t
  dequeue : t -> t * int
end
```

```
structure naive_queue : Queue = struct
  type t = List int

  enqueue x q = Cons(x, q)
  dequeue q = match q with ...
end
```

Step 2: Dependency Abstraction 🤖

implementation view

```
signature Queue = sig
```

```
  type t = List int
```

```
  enqueue : int -> List int -> List int
```

```
  dequeue : List int -> List int * int
```

```
end
```

```
structure naive_queue : Queue = struct
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  type t = List int
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  enqueue x q = Cons(x, q)
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  dequeue q = match q with ...
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end
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Step 3: Our New Password Checker 🎉

```
signature PasswordChecker = sig
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  pass : [pwd] string
  check : [ $\alpha$ ] string -> [ $\alpha$ ] bool

  encrypt : [pwd  $\alpha$ ] string -> [ $\alpha$ ] string

end
```

Step 3: Our New Password Checker 🎉

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```
structure pc : PasswordChecker = struct
  dependency pwd = [ ]

  pass : [pwd] string = "katya"
  check : [ $\alpha$ ] string -> [ $\alpha$ ] bool
    = fun attempt -> attempt == pass
  encrypt : [pwd  $\alpha$ ] string -> [ $\alpha$ ] string

end
```

Step 3: Our New Password Checker 🎉

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structure pc : PasswordChecker = struct
  dependency pwd = [ ]

  pass : [pwd] string = "katya"
  check : [ $\alpha$ ] string -> [ $\alpha$ ] bool
    = fun attempt -> attempt == pass
  encrypt : [pwd  $\alpha$ ] string -> [ $\alpha$ ] string
    = fun str -> gpg str
end
```

Step 3: Our New Password Checker 🎉

```
structure pc : PasswordChecker = struct
  dependency pwd = [ ]

  pass : [pwd] string = "katya"
  check : [ $\alpha$ ] string -> [ $\alpha$ ] bool
    = fun attempt -> attempt == pass
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    = fun str -> gpg str
end
```

Extra: Dependency Elision

`incr : [α] int -> [α] int`

`add : [α] int -> [β] int -> [α β] int`

Extra: Dependency Elision

`incr : int -> int`

`add : $[\alpha]$ int -> $[\beta]$ int -> $[\alpha \beta]$ int`

Extra: Dependency Elision

```
incr : int -> int
```

```
add  : int -> int -> int
```


Extra: Dependency Elision

`incr : int -> int`

`add : int -> int -> int`

`map : ($\alpha \rightarrow \beta$) -> list α -> list β`

`fold : $\beta \rightarrow (\alpha \rightarrow \beta \rightarrow \beta) \rightarrow$ list $\alpha \rightarrow \beta$`

`filter : ($\alpha \rightarrow [\beta]$ bool) -> list $\alpha \rightarrow [\beta]$ list α`

Extra: Dependency Elision

`incr : int -> int`

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`fold : $\beta \rightarrow (\alpha \rightarrow \beta \rightarrow \beta) \rightarrow$ list $\alpha \rightarrow \beta$`

`filter : ($\alpha \rightarrow [\beta]$ bool) -> list $\alpha \rightarrow [\beta]$ list α`

Full explanation + more goodies in the paper!

Takeaway: Full-strength **non-interference** and **practical programming** are perfectly aligned.

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